Practice with Examples

For use with pages 291-298

GOAL

Solve quadratic equations using the quadratic formula

VOCABULARY

The quadratic formula,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a},$$

is used to find the solutions of the quadratic equation $ax^2 + bx + c = 0$, when $a \neq 0$.

The expression $b^2 - 4ac$, where a, b, and c are coefficients of the quadratic equation $ax^2 + bx + c = 0$, is called the **discriminant.**

If $b^2 - 4ac > 0$, then the equation has two real solutions.

If $b^2 - 4ac = 0$, then the equation has one real solution.

If $b^2 - 4ac < 0$, then the equation has two imaginary solutions.

EXAMPLE 1

Solving a Quadratic Equation with Two Real Solutions

Solve
$$-8x^2 - 5x = -x^2 - 1$$
.

SOLUTION

$$-8x^{2} - 5x = -x^{2} - 1$$

$$-7x^{2} - 5x + 1 = 0$$

$$x = \frac{5 \pm \sqrt{(-5)^{2} - 4(-7)(1)}}{2(-7)}$$

$$x = \frac{5 \pm \sqrt{53}}{-14}$$

Quadratic formula with
$$a = -7$$
, $b = -5$, and $c = 1$.

The solutions are

$$x = \frac{5 + \sqrt{53}}{-14} \approx -0.88$$
 and $x = \frac{5 - \sqrt{53}}{-14} \approx 0.16$.

Exercises for Example 1

Use the quadratic formula to solve the equation.

1.
$$x^2 - 9x + 5 = 0$$

2.
$$5x^2 + 3x - 1 = 0$$

$$3. -x^2 + 2x + 4 = 0$$

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EXAMPLE 2

Solving a Quadratic Equation with One Real Solution

Solve
$$2x^2 - 5x + 7 = x^2 - 3x + 6$$
.

SOLUTION

$$2x^{2} - 5x + 7 = x^{2} - 3x + 6$$

$$x^{2} - 2x + 1 = 0$$

$$x = \frac{2 \pm \sqrt{(-2)^{2} - 4(1)(1)}}{2(1)}$$

$$x = \frac{2 \pm \sqrt{0}}{2}$$

Write in standard form.

Write original equation.

Quadratic formula with a = 1, b = -2, and c = 1.

Simplify.

Simplify.

The solution is 1.

Exercises for Example 2

x = 1

Use the quadratic formula to solve the equation.

4.
$$x^2 - 6x + 9 = 0$$

5.
$$x^2 + 4x + 4 = 0$$

6.
$$x^2 + 10x + 25 = 0$$

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EXAMPLE 3

Solving a Quadratic Equation with Two Imaginary Solutions

Solve $3x^2 - 3x + 5 = 0$.

SOLUTION

$$3x^{2} - 3x + 5 = 0$$

$$x = \frac{3 \pm \sqrt{(-3)^{2} - 4(3)(5)}}{2(3)}$$

$$x = \frac{3 \pm \sqrt{-51}}{6}$$

$$x = \frac{3 \pm i\sqrt{51}}{6}$$

Write original equation.

Quadratic formula with a = 3, b = -3, and c = 5.

Simplify.

Write using the imaginary unit i.

The solutions are $\frac{1}{2} + \frac{\sqrt{51}}{6}i$ and $\frac{1}{2} - \frac{\sqrt{51}}{6}i$.

Exercises for Example 3

Use the quadratic formula to solve the equation.

7.
$$x^2 - 6x = -10$$

8.
$$x^2 = -x - 1$$

9.
$$x^2 - 2x + 3 = 0$$